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**ADDITIONAL MATHEMATICS**

**0606/22**

Paper 2

**October/November 2016**

MARK SCHEME

Maximum Mark: 80

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**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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### Abbreviations

|      |                            |
|------|----------------------------|
| awrt | answers which round to     |
| cao  | correct answer only        |
| dep  | dependent                  |
| FT   | follow through after error |
| isw  | ignore subsequent working  |
| oe   | or equivalent              |
| rot  | rounded or truncated       |
| SC   | Special Case               |
| soi  | seen or implied            |
| www  | without wrong working      |

| Question | Answer  | Marks  | Part Marks   |
|----------|---|--|--|
| <b>1</b> | $4x - 3 = x \rightarrow x = 1$<br>$4x - 3 = -x$<br>$x = 0.6$<br><br><b>OR</b> $(4x - 3)^2 = x^2$<br>$15x^2 - 24x + 9 = 0$<br>$3(x - 1)(5x - 3) = 0$<br>$x = 1$ and $x = 0.6$                        | <b>B1</b><br><b>M1</b><br><b>A1</b><br><br><b>B1</b><br><b>M1</b><br><b>A1</b> | www<br>use of $-x$ or $-(4x - 3)$ but not both.<br><br>solve correct 3 term quadratic<br>www   |
| <b>2</b> | $a(\sqrt{3} - 1) + b(\sqrt{3} + 1)$<br>$= (\sqrt{3} - 3)(\sqrt{3} - 1)(\sqrt{3} + 1)$<br>$= 2(\sqrt{3} - 3)$ oe<br><br>$a + b = 2$<br>$-a + b = -6$<br><br>$b = -2$ and $a = 4$                     | <b>M1</b><br><br><br><b>DM1</b><br><b>A1</b><br><b>DM1</b><br><b>A1</b>        | Common denominator or<br>$\times (\sqrt{3} - 1)(\sqrt{3} + 1)$<br><br>equate constant terms and $\sqrt{3}$ terms.<br>both correct<br>solve two <b>linear</b> equations to obtain $a =$ or<br>$b =$<br>both correct |
| <b>3</b> | $2\lg x = \lg x^2$<br>$1 = \lg 10$<br>$\lg x^2 - \lg\left(\frac{x+10}{2}\right) = \lg\left(\frac{2x^2}{x+10}\right)$ oe<br>$2x^2 - 10x - 100 = 0 \rightarrow 2(x+5)(x-10) = 0$<br><br>$x = 10$ only | <b>B1</b><br><b>B1</b><br><b>B1</b><br><b>M1</b><br><b>A1</b>                  | soi anywhere<br>soi anywhere<br><br>soi division; logs may be removed<br><br>obtain correct 3 term quadratic equation and attempt to solve<br>$x = -5$ must not remain.  |

| <b>Question</b> | <b>Answer</b>  | <b>Marks</b>   | <b>Part Marks</b>  |
|-----------------|--|--|--|
| <b>4 (i)</b>    | $t = 10 \rightarrow N = 7000 + 2000e^{-0.5}$<br>$= 8213$ or 8210   | <b>B1</b>  | Do not accept non integer responses.   |
| <b>(ii)</b>     | $N = 7500 \rightarrow 7500 = 7000 + 2000e^{-0.05t}$<br>$e^{-0.05t} = \frac{500}{2000}$<br>$-0.05t = \ln 0.25 \rightarrow t = \frac{\ln 0.25}{-0.05}$<br>$= 27.7$ (days)  | <b>M1</b><br><br><b>M1</b><br><b>A1</b>                  | insert and make $e^{-0.05t}$ subject<br><br>take logs and make $t$ the subject<br>awrt 27.7  |
| <b>(iii)</b>    | $\frac{dN}{dt} = -100e^{-0.05t}$<br>$t = 8 \rightarrow \frac{dN}{dt} = \pm 67$ (.0)  | <b>M1</b><br><b>A1</b><br><b>A1</b>                      | $ke^{-0.05t}$ where $k$ is a constant<br>$k = -100$ or $-0.05 \times 2000$<br>awrt $\pm 67$ mark final answer  |
| <b>5 (i)</b>    | $\frac{dy}{dx} = 3x^2 + 4x - 7$<br>$x = -2 \rightarrow \frac{dy}{dx} = 12 - 8 - 7 = -3$<br><br>Equation of tangent :<br>$\frac{y-16}{x+2} = -3 \rightarrow y = -3x + 10$   | <b>B1</b><br><br><b>M1</b><br><br><b>A1</b>              | insert $x = -2$ into <i>their</i> gradient and use $(-2, 16)$ and <i>their</i> gradient of tangent in equation of line.  |
| <b>(ii)</b>     | Tangent cuts curve again<br>$x^3 + 2x^2 - 7x + 2 = -3x + 10$<br>$x^3 + 2x^2 - 4x - 8 = 0$<br>$(x+2)(x+2)(x-2) = 0$<br><br>$x = 2, y = 4$   | <b>M1</b><br><b>A1</b><br><b>M1</b><br><b>A1A1</b>       | equate curve and <i>their</i> linear answer from (i).<br><br>factorise: $(x \pm 2)$ and a two or three term quadratic is sufficient. Allow long division withhold final <b>A1</b> if $(2, 4)$ not clearly identified as their sole answer. |
| <b>6 (i)</b>    | $\frac{\cos x}{1 + \tan x} - \frac{\sin x}{1 + \cot x} = \frac{\cos x}{1 + \frac{\sin x}{\cos x}} - \frac{\sin x}{1 + \frac{\cos x}{\sin x}}$<br><br>$= \frac{\cos^2 x}{\cos x + \sin x} - \frac{\sin^2 x}{\cos x + \sin x}$<br><br>$= \frac{(\cos x - \sin x)(\cos x + \sin x)}{(\cos x + \sin x)}$ | <b>M1</b><br><br><b>M1</b><br><b>A1</b><br><br><b>A1</b> | $\tan x = \frac{\sin x}{\cos x}$ and $\cot x = \frac{\cos x}{\sin x}$<br><br>Attempt to multiply by $\cos x$ and $\sin x$<br><br>AG  |
| <b>(ii)</b>     | $-\sin x + \cos x = 3\sin x - 4\cos x$<br>$5\cos x = 4\sin x$<br>$\tan x = \frac{5}{4}$<br>$x = 51.3^\circ, -128.7^\circ$  | <b>M1</b><br><br><b>A1</b><br><b>A1A1</b>                | equate and collect $\sin x$ and $\cos x$ oe<br><br><b>FT</b> from $\tan x = k$   |

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| Question | Answer  | Marks  | Part Marks  |
|----------|---|--|---|
| 7 (i)    | $h = \sqrt{9 - x^2}$ $A = \frac{\sqrt{9 - x^2}}{2}(14 + x + x) = \sqrt{9 - x^2}(7 + x)$   | <b>B2/1/0</b>  | Must be clear that $\sqrt{9 - x^2}$ is the height of the trapezium. $14 + 2x$ oe must be seen AG  |
| (ii)     | $\frac{dA}{dx} = \sqrt{9 - x^2} + (7 + x) \frac{1}{2}(9 - x^2)^{-0.5} \times -2x$ $\frac{dA}{dx} = 0 \rightarrow 9 - x^2 = 7x + x^2$ $2x^2 + 7x - 9 = 0$ $x = 1$ $A = 16\sqrt{2} \text{ or } 8\sqrt{8} \text{ or } \sqrt{512} \text{ or } 22.6$ | <b>M1</b><br><b>A2/1/0</b><br><br><b>M1</b><br><b>A1</b><br><b>A1</b><br><b>A1</b> | product rule on correct function<br>minus 1 each error, allow unsimplified.<br><br>equate to 0 and simplify to a linear or quadratic equation.<br>correct three term quadratic obtained<br><br>Extra positive answer loses penultimate <b>A1</b> .<br>ignore negative solution. |
| 8 (i)    | $f'(x) = \frac{(x^3 + 1)9x^2 - (3x^3 - 1)3x^2}{(x^3 + 1)^2}$ $= \frac{12x^2}{(x^3 + 1)^2}$  | <b>M1</b><br><b>A1</b><br><br><b>A1</b>  | quotient rule or product rule<br>all correct<br><br>www beware $9x^6 - 9x^6$ gets <b>A0</b>   |
| (ii)     | $\int_1^2 \frac{x^2}{(x^3 + 1)^2} dx = \frac{1}{12} \left[ \frac{3x^3 - 1}{x^3 + 1} \right]_1^2$ $= \frac{1}{12} \left[ \frac{23}{9} - \frac{2}{2} \right]$ $= \frac{7}{54}$  | <b>M1</b><br><b>A1</b><br><br><b>DM1</b><br><br><b>A1</b>                          | $c \times \frac{3x^3 - 1}{x^3 + 1}$<br><b>FT</b> $c = \frac{1}{\text{their } 12}$<br><br>top limit – bottom limit in <i>their</i> integral.<br><br>or 0.130 or 0.1296 or 0.12   |
| (iii)    | $x = \frac{3y^3 - 1}{y^3 + 1}$ $y^3 = \frac{x + 1}{3 - x}$ $f^{-1}(x) = \sqrt[3]{\frac{x + 1}{3 - x}}$ $\text{Domain : } -1 \leq x \leq 2\frac{6}{7}$   | <b>B1</b><br><br><b>B1</b><br><br><b>B1</b><br><b>B1</b><br><b>B1</b>              | make $y^3$ or $x^3$ the subject<br><br><b>FT</b> take cube root (as long as $y^3$ or $x^3$ equals a fraction with terms in $x$ or $y$ only) oe<br><b>FT</b> change $x$ and $y$ – can be done at any time<br>Allow upper limit of 2.86. Do not isw                               |

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| Question | Answer   | Marks                                      | Part Marks  |
|----------|--|--|---|
| 9 (i)    | tangent touches circle<br>$x^2 + (kx - 4)^2 - 2(kx - 4) = 8$<br>$k^2x^2 + x^2 - 8kx - 2kx + 16 = 0$ or better  | M1<br>A1                                   | eliminate $y$ or $x$ allow unsimplified   |
|          | Equal roots as tangent touches circle :<br>$b^2 = 4ac$<br>$(-10k)^2 = 4(k^2 + 1) \times 16$<br>$36k^2 = 64$<br>$k = +\frac{4}{3}$ only   | DM1<br>A1<br>A1                            | use of discriminant on 3 term quadratic so<br>oe any inequality loses last A1   |
|          | (ii)<br>$x = \frac{-b}{2a} \rightarrow x = \frac{\frac{4}{3} \times 10}{\frac{25}{9}}$<br>$x = \frac{12}{5} \quad y = -\frac{4}{5}$<br><b>OR</b> tangent $y = \frac{4}{3}x - 4$ cuts radius<br>$y = -\frac{3}{4}x + 1$<br>at $x = \frac{12}{5}$<br>$y = -\frac{4}{5}$<br><b>OR</b> Obtain $25x^2 - 120x + 144 = 0$ oe<br>$(5x - 12)(5x - 12) = 0$<br>$x = \frac{12}{5} \rightarrow y = -\frac{4}{5}$ | M1<br>A1A1<br>M1<br>A1<br>A1<br>M1<br>A1A1 | use $x = \frac{-b}{2a}$<br>find equation of radius and attempt to solve with tangent<br>obtain any 3 term quadratic using <i>their</i> non zero $k$ and reach $x = \dots$ |
| (iii)    | $TP = \sqrt{(0 - 2.4)^2 + (-4 + 0.8)^2} = 4$   | M1A1                                       | M1 for using <i>their</i> $T$ and $(0, -4)$ .<br>Signs must be correct.   |

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|--------|---|----------|-------|
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| Question | Answer   | Marks                                | Part Marks   |
|----------|--|--------------------------------------|--|
| 10 (i)   | $r_j = \begin{pmatrix} 5000 \\ 1000p \end{pmatrix} + \begin{pmatrix} -2\cos 40 \\ 2\cos 50 \end{pmatrix} t$  | B1<br>B1                             | x coordinate oe<br>y coordinate oe   |
| (ii)     | $2.5t\cos 70 = 5000 - 2t\cos 40$<br>$t = \frac{5000}{2.5\cos 70 + 2\cos 40}$<br>$= 2095$ awrt or 2090 or 2100<br>$(2.5\cos 20 - 2\cos 50) \times 2095 = 1000p$<br>$p = 2.23$ awrt  | M1<br>DM1<br>A1<br>M1<br>A1          | equate <i>their</i> x values (must be 3 terms)<br>make <i>t</i> the subject allow one sign error<br>equate <i>their</i> y values (must be 3 terms) and insert <i>their</i> <i>t</i> or $ t $ . |
| 11 (i)   | Free choice : no. of ways<br>${}^6C_4 \times {}^5C_2 = 15 \times 10$<br>$= 150$  | B1<br>B1                             | ${}^6C_4 \times$ another ${}^nC_r$ term only<br>$\times {}^5C_2$ and answer or vice versa  |
| (ii)     | Both Mr and Mrs Coldicott<br>${}^5C_3 \times {}^4C_1 = 10 \times 4$<br>$= 40$  | B1<br>B1                             | ${}^5C_3 \times$ another ${}^nC_r$ term only<br>$\times {}^4C_1$ and answer or vice versa  |
| (iii)    | Mr C and not Mrs C ${}^5C_3 \times {}^4C_2 (= 60)$<br>Not Mr C and Mrs C ${}^5C_4 \times {}^4C_1 (= 20)$<br>Total = 80<br><br><b>OR</b><br>Total = (i) – (ii) – neither<br>Neither = ${}^5C_4 \times {}^4C_2 = 30$<br>Total = $150 - 40 - 30 = 80$ | B1<br>B1<br>B1<br><br>M1<br>A1<br>A1 | An incorrect final answer does not affect the awarding of the first two B1 marks.<br><br>www   |